

WE CLAIM

1. A method of elliptic curve encryption comprising the step of:
 - (a) selecting an elliptic curve $E_p(a,b)$ of the form $y^2 = x^3 + ax + b \pmod{p}$ wherein a and b are non-negative integers less than p satisfying the formula $4a^3 + 27b^2 \pmod{p}$ not equal to 0;
 - 5 (b) generating a large 160 bit random number by a method of concatenation of a number of smaller random numbers;
 - (c) generating a well hidden point $G(x,y)$ on the elliptic curve $E_p(a,b)$ by scalar multiplication of a point $B(x,y)$ on the elliptic curve with a large random integer which further comprises the steps:
 - 10 (i) converting the large random integer into a series of powers of 2^{31} ;
 - (ii) converting each coefficient of 2^{31} obtained from above step into a binary series;
 - (iii) multiplication of binary series obtained from steps(i) & (ii) above with the point $B(x,y)$ on the elliptic curve
 - 15 (d) generating a private key n_A (of about ≥ 160 bit length);
 - (e) generating of public key $P_A(x,y)$ given by the formula $P_A(x,y) = (n_A \cdot G(x,y)) \pmod{p}$;
 - (f) encrypting the input message MSG;
 - (g) decrypting the ciphered text
- 20 2. A method of elliptic curve encryption as claimed in claim 1, wherein the said number p appearing in selection of elliptic curve is about 160 bit length prime number.
3. A method of elliptic curve encryption as claimed in claim (1), wherein the said method of generating any large random integer M comprises the steps of;
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- (i) setting $l = 0$;
 - (ii) setting M to null;
 - (iii) determining whether $l < 6$;
 - (iv) going to next if true;
 - 5 (v) returning M as result if false;
 - (vi) generating a random number Rl within $(0,1)$ by using library function;
 - (vii) multiplying Rl with 10^9 to obtain $BINT$ – an integer of size 9 digits;
 - (viii) concatenating $BINT$ to M ;
 - 10 (ix) setting $l = l + 1$;
 - (x) returning to step (iii)
4. A method of elliptic curve encryption as claimed in claims 1 to 3 wherein the said conversion of large random integer into a series of powers of 2^{31} and said conversion of each coefficient m_n of the said 2^{31} series thus obtained for scalar multiplication for the said
- 15 random integer with the said point $B(x,y)$ on the said elliptic curve $E_p(a,b)$ comprises the steps of:
- (i) accepting a big integer M ;
 - (ii) setting $T31$ equal to 2^{31} .
 - 20 (iii) setting $LIM = \text{size of } M \text{ (in bits)}$ and initializing array $A()$ with size LIM ;
 - (iv) setting $INCRE$ equal to zero;
 - (v) setting N equal to $M \text{ modulus } T31$;
 - (vi) setting $M = \text{INT}(M/T31)$;
 - 25 (vii) determining whether N is equal to 0;
 - (viii) going to next if true;
 - (ix) going to step (xxiv) if false;
 - (x) determining whether M is equal to 0;
 - (xi) going to next if true;

- (xii) going to step (xxvi) if false;
- (xiii) setting $I = 0$ & $J = 0$;
- (xiv) determining whether $I \geq LIM$;
- (xv) going to next step if false;
- 5 (xvi) going to step (xxviii) if true;
- (xvii) determining whether $A(I)$ is equal to 1;
- (xviii) going to next step if true;
- (xix) returning to step (xii) if false;
- (xx) setting $B(J) = I$;
- 10 (xxi) incrementing J by 1;
- (xxii) incrementing I by 1;
- (xxiii) returning to step (xiv);
- (xxiv) calling function **B SERIES** (N , $INCRE$) and updating array $A()$;
- (xxv) returning to step (x)
- 15 (xxvi) setting $INCRE = INCRE + 31$;
- (xxvii) returning to step (v);
- (xxviii) returning array $B()$ as result.

5. A method of elliptic curve encryption as claimed in claims 1 to 4, wherein the said conversion of large random integer into a series of powers of 2^{31} and said conversion of each coefficient m_n of the said 2^{31} series thus obtained for the said scalar multiplication of the said random integer with the said point $B(x,y)$ on the said elliptic curve $E_p(a,b)$ further comprises the steps of:

- (i) accepting N and $INCRE$;
- 25 (ii) assigning **BARRAY** as an array of values which are powers of $2(2^0, \dots, 2^{30})$;
- (iii) setting $SIZE = \text{size of } N \text{ (in digits)}$;
- (iv) computing $POINTER = 3(SIZE) + \text{INT}(SIZE/3) - 4$;
- (v) determining whether $POINTER < 2$;
- 30 (vi) going to next if true;

- (vii) going to step (ix) if false;
 - (viii) setting POINTER equal to zero;
 - (ix) determining whether $(BARRAY(POINTER) \geq N)$;
 - (x) going to next step if true;
 - 5 (xi) going to step (xx) if false;
 - (xii) determining whether $BARRAY(POINTER) = N$;
 - (xiii) going to next step if true;
 - (xiv) going to step (xvii) if false;
 - (xv) setting $A(POINTER + INCRE)$ equal to 1;
 - 10 (xvi) returning array A () as result;
 - (xvii) setting $A((POINTER - 1) + INCRE)$ equal to 1;
 - (xviii) computing $N = N - BARRAY(POINTER - 1)$;
 - (xix) returning to step (iii);
 - (xx) setting $POINTER = POINTER + 1$;
 - 15 (xxi) returning to step (ix);
6. A method of elliptic curve encryption as claimed in claims 1 to 5, wherein the said scalar multiplication of the said binary series with the said point $B(x,y)$ on the said elliptic curve $E_p(a,b)$ comprises the steps of:
- 20 (i) accepting $B(x,y)$, a point on $E_p(a,b)$;
 - (ii) accepting array B() with size LIM;
 - (iii) setting $I = 0$ & $J = 0$;
 - (iv) determining whether $B(J) = I$;
 - (v) going to next step if true;
 - 25 (vi) going to step (xxv) if false;
 - (vii) setting $PARR(x,y)(J)$ equal to $B(x,y)$;
 - (viii) Incrementing J by 1;
 - (ix) determining whether J is equal to LIM;
 - (x) going to next step if true;

- (xi) going to step (xxv) if false;
- (xii) setting $K=zero$;
- (xiii) determining whether $K>0$;
- (xiv) going to next step if true;
- 5 (xv) going to step (xii) if false;
- (xvi) computing $FP(x,y)=FP(x,y) + PARR(x,y) (K)$;
- (xvii) incrementing K by 1;
- (xviii) determining whether $K=LIM$;
- (xix) going to next if true;
- 10 (xx) returning to step (xiii) if false;
- (xxi) returning $FP(x,y)$ as result;
- (xxii) setting $FP(x,y)$ equal to $PARR(x,y) (K)$;
- (xxiii) incrementing K by 1;
- (xxiv) returning to step (xiii);
- 15 (xxv) Incrementing I by 1;
- (xxvi) setting $B(x,y) = B(x,y) + B(x,y)$;
- (xxvii) returning to step (iv)..

- 7. A method of elliptic curve encryption as claimed in claim 1, wherein the said public key $P_A(x,y)$ is also a point on the said elliptic curve $E_p(a,b)$.
- 20 8. A method of elliptic curve encryption as claimed in claims 1 to 7, wherein the said generation of the said private key n_A and the said public key $P_A(x,y)$ comprises the steps of:
 - (i) entering a big odd integer p of size ≥ 160 bits;
 - 25 (ii) determining whether p is a prime number;
 - (iii) going to next step if p is prime;
 - (iv) going to step (xix) if p is not prime;
 - (v) entering a small integer $a > 0$;
 - (vi) setting integer $b = 0$ & $x = 1$;

- (vii) determining whether $4a^3 + 27b^2 \bmod(p) = \text{zero}$;
- (viii) going to next step if false;
- (ix) incrementing b by 1 if true and going to step (vii);
- (x) setting $z (=y^2) = x^3 + ax + b$;
- 5 (xi) determining whether $z (=y^2)$ is a perfect square;
- (xii) going to step (xxi) if z is not a perfect square;
- (xiii) setting B(x,y) equal to (x,y) if z is a perfect square;
- (xiv) selecting a large random integer r_1 ;
- (xv) setting $G(x,y) = (r_1 \cdot B(x,y)) \bmod(p)$;
- 10 (xvi) selecting a large random integer n_A ;
- (xvii) setting $P_A(x,y) = (n_A \cdot G(x,y)) \bmod(p)$;
- (xviii) return $P_A(x,y)$ as public key and n_A as private key;
- (xix) incrementing p by 2;
- (xx) returning to step (ii);
- 15 (xxi) Incrementing x by 1;
- (xxii) determining whether $x > 900$;
- (xxiii) going to next step if true;
- (xxiv) going to step (x) if false;
- (xxv) Incrementing b by 1;
- 20 (xxvi) setting $x = 1$;
- (xxvii) returning to step (vi).

9. A method of elliptic curve encryption as claimed in claims 1 to 8, wherein the said encryption of the said message MSG comprises the steps of:

- 25 (i) generating a large random integer K;
- (ii) setting $P_{\text{mask}}(x,y) = k \cdot P_A(x,y) \bmod(p)$;
- (iii) setting $P_k(x,y) = k \cdot G(x,y) \bmod(p)$;
- (iv) accepting the message to be encrypted (MSG);
- (v) converting the message into a point $P_c(x,y)$;

- (vi) generating a random point $P_m(x,y)$ on elliptic curve $E_p(a,b)$;
- (vii) setting $P_a(x,y) = (P_c(x,y) - P_m(x,y))$;
- (viii) setting $P_{mk}(x,y) = (P_m(x,y) + P_{mask}(x,y)) \bmod(p)$;
- (ix) returning $P_k(x)$, $P_a(x,y)$ and $p_{mk}(x)$ as the result (cipher).

5 10. A method of elliptic curve encryption as claimed in claim 1 to 9, wherein the said decryption of the said ciphered text comprises the steps of:

- (i) getting cipher text $(P_k(x), P_a(x,y), P_{mk}(x))$;
- (ii) computing $P_k(y)$ from $P_k(x)$ using elliptic curve $E_p(a,b)$;
- 10 (iii) computing $P_{mk}(y)$ from $P_{mk}(x)$ using elliptic curve $E_p(a,b)$;
- (iv) computing $P_{ak}(x,y) = (n_A \cdot P_k(x,y)) \bmod(p)$;
- (v) computing $P_m(x,y) = (P_{mk}(x,y) - P_{ak}(x,y)) \bmod(p)$;
- (vi) computing $P_c(x,y) = P_m(x,y) + P_a(x,y)$;
- (vii) converting $P_c(x,y)$ into the input message MSG.

15 11. A method of elliptic curve encryption substantially as described and illustrated herein.